Nano-Dielectric Resonator Antenna Reflectarray/Transmittarray for Terahertz Applications

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Abstract

Nanoantennas have been introduced for different applications as solar-cell, medical imaging, and fast data communications. The material properties of good conducting metals introduce plasmonic behavior at terahertz frequencies. The electrical properties of different good conducting metals are modeled using the Drude model and have been investigated for reflectarray/ transmittarray operation. The radiation characteristics of nano-dielectric resonator antenna (NDRA) reflectarray at 633 nm have been investigated. The unit-cell consists of NDR mounted on the metallic supporting plane. A parametric study for the NDR unit cell dimensions and material has been introduced. The NDR unit-cell with silver supporting plane has been designed and analyzed for reflectarray applications at 633 nm. The radiation characteristics of the NDRA transmittarray has been introduced for 633 nm applications. The NDR unit-cell consists of two NDRs mounted on the top and bottom of the metallic supporting plane. A comparison between the radiation characteristics of 17×17 and 21×21 NDRA transmittarray has been introduced. A compromise between the nano-transmittarray size, maximum gain, and operating bandwidth is applied to terahertz applications. The finite integral technique is used to carry a full wave analysis to design an NDRA reflectarray and an NDRA transmittarray.

1. Introduction

The radiation characteristics of a conventional radio-frequency (RF) antenna have been presented in detail in [1]. Nanoantenna is a resonant device, which converts the electromagnetic wave into a localized energy at terahertz frequencies [2]. Recently, wide bandwidth nanoantennas have been introduced for faster information exchange. Nanoantennas have many applications including solar cells, on-chip wireless optical communication and biological imaging. Different forms of the microwave antennas such as dipole, monopole, Yagi-Uda, and bow-tie antenna have been investigated at the terahertz frequencies [3-6] which focus on resonant metallic nanostructures. The materials used for nanoantennas fabrication are generally good conducting metals such as gold and silver [7]. The resonant structures of good conducting metals show electromagnetic resonances, when being excited by an incident light, this is called surface plasmon polariton resonances (SPPRs). The electrical properties of these metals are described by the Drude-Lorentz model which considers both the free electrons contributions and harmonic oscillator SPPRs contributions [8].

The optical properties of the nanoantenna depend on the size, geometry and material. However, only the high ohmic losses of metals at terahertz frequencies affect the radiation efficiency of nanoantennas [2]. The nanoantenna resonance length is not determined by the free space wavelength, but by the SPP wavelength in the metal [2]. The current distribution on the nanoantenna has a standing wave pattern similar to that of the RF antennas, but with non-uniform spacing between subsequent current lobes. Nanoantenna arrays introduce a superior directivity, field confinement, absorption cross-section and flexibility in beam shaping compared with single nanoantennas. Dielectric resonator antennas (DRA) have many attractive features and applications at microwave frequencies [9]. The DRAs have different shapes as a hemisphere, cylinder, or rectangular and are typically mounted on a metal layer regarded as perfect electric conductor. The DRAs are generally constructed from low-loss high-permittivity dielectric materials (up to \( \varepsilon_r =100 \)). To increase the efficiency of resonant nanoantennas the low-loss high-permittivity dielectric materials available at terahertz frequencies are used. At terahertz frequencies, the wave penetrates the metals due to the plasmonic effect and the antenna scaling property is not valid. The radiation characteristics of the DRA at 633 nm have been investigated in [10]. High-gain microwave antennas have been used in many applications such as radar and satellite communications. The parabolic reflector and phased array antenna have high gain, narrow main lobe and high power capacity, but they suffer some disadvantages as high cost, and large volume for the parabolic reflector, and lossy feed networks in a phased array. Reflectarray antenna combines the advantages of parabolic reflector and phased array and overcomes their disadvantages [11]. The reflectarray antenna consists of a primary source illuminating a planar surface composed of an array of unit-cells. The phase shift of each unit-cell is adjusted to collimate the reflected wave in the desired direction. Reflectarray suffer from feeder blocking effect, so
it requires an offset feed to avoid blockage losses, which leads to destroying the symmetry of the antenna aperture and increases the angle of incidence of some individual elements [12]. The transmitarray overcomes reflectarray feed blocking problem, and both the reflectarray and transmitarray transform the spherical wave emanating from the feeder into a plane wave. Transmitarray is similar to the reflectarray, but the incident wave is not reflected but passes through the antenna structure as it is collimated into a plane wave on the other side. 9x9 unit-cells elements, nano-reflectarray using single perforated silver sheet at 735 THz has been introduced [13]. A detailed analysis of the radiation characteristics of nano-dielectric resonator antenna single element and the NDRA reflectarray at 633 nm is investigated in [10]. A circularly polarized graphene transmitarray for terahertz application has been presented in [14].

In this paper, the electrical material properties of metals at terahertz frequencies have been determined. A parametric study of the NDRA unit-cell for reflectarray at 633 nm has been introduced. The effect of changing the metal material property on the performance of the NDRA unit-cell is investigated. A 21x21 unit-cell elements NDRA reflectarray has been designed and analyzed using the finite integral technique based on the commercial software CST microwave studio [15, 16]. A parametric study of an NDRA unit-cell with the silver supporting plane for transmitarray operating at 633 nm has been proposed. The radiation characteristics of the 21x21 NDRA transmitarray are determined and compared to a 17x17 NDRA transmitarray.

2. Material properties at Terahertz range

At terahertz frequencies, the behaviour of conventional metals properties behaves in a different way compared to the microwave frequencies [7]. In microwave frequency range the electric field inside the conductors is zero, which leads to perfect reflection from the surface of the metal, as the conductivity of metal is very high. However, at terahertz frequencies, the assumption of perfect conductor metals is not valid and the losses cannot be neglected [8]. The material properties in the terahertz range can be described by a free electron gas moving through a lattice of positive ions. The frequency dependent complex permittivity and the electrical conductivity of metal in the terahertz frequency range is described using the Drude model given by [8]

\[
\varepsilon = \varepsilon_1 + j\varepsilon_2 = \varepsilon_0 \left[1 - \frac{\omega^2}{\omega_p^2 - j\omega\gamma}\right]
\]

(1)

\[
\sigma = \sigma_1 + j\sigma_2 = \frac{\varepsilon_0 \omega_p^2}{\omega}\gamma
\]

(2)

where \(\varepsilon_1\) is the real part of permittivity and is a measure of how much energy from an external field is stored in a material, \(\varepsilon_2\) is the imaginary part of permittivity (loss factor) and is a measure of how dissipative or lossy a material is to an external field, \(\varepsilon_0\) is the dielectric constant of vacuum, \(\omega\) is the angular frequency of the electromagnetic wave,

\(\gamma\) is the angular collision frequency, and \(\omega_p\) is the electron plasma angular frequency [8]

\[
\omega_p = \sqrt{n_e e^2 / \varepsilon_0 m_e} = 56.40 \sqrt{n_e}
\]

(3)

where \(n_e\) is the free electron density, \(m_e\) is the electron mass, and \(q\) is the charge of the electron. Figure 1 shows the variation of electric permittivity \(\varepsilon\), and the conductivity \(\sigma\), versus frequency in the terahertz range of gold, copper, silver and aluminum. The electrical permittivity and conductivity of all metals take an exponential variation with frequency. \(\varepsilon_1\) and \(\sigma_1\) (the permittivity components of \(\varepsilon\) and \(\sigma\)) are increased by increasing frequency (negative with reduced magnitude with higher frequency) while \(\varepsilon_2\) and \(\sigma_1\) (the conductivity components with \(\sigma_1\) normally dominating at lower frequencies) are decreased in magnitude by increasing frequency. The skin depth \(\delta(\omega)\) represents how deep the electromagnetic wave can penetrate the material surface (1/e of its initial value at the surface) [8]

\[
\delta(\omega) = \frac{2c}{\omega \varepsilon_0}
\]

(4)

where \(c\) is the speed of light. The variation of skin- depth versus frequency for different metals is shown in Fig.2. At 474 THz, the skin depth is 32 nm for gold, 28 nm for copper, 24.5 nm for silver and 17 nm for aluminum.

![Figure 1](image)

**Figure 1** The variations of complex permittivity and electrical conductivity versus frequency for different types of metals.
The reflectarray/transmitarray configuration. For the reflectarray/transmitarray located in x-y plane the wave is reflected/transmitted from each unit-cell at direction \((\theta_d, \varphi_d)\) suffer from additional phase shift due to the position of the element in the array (\(x_{cij}, y_{cij}\)) and spacing between the cell element and the feeding horn \(d_{ij}\) as shown in Fig. 3. To collimate the reflected/transmitted wave at direction \((\theta_d, \varphi_d)\) each unit-cell requires a compensation phase
\[
\varphi_{ij}(x_{cij}, y_{cij}) = k_0 d_{ij} + \varphi_{cij}
\]
where \(k_0 = 2\pi/\lambda\) is the wave number, \(d_{ij}\) is the distance from the feeding horn to each unit cell [12]
\[
d_{ij} = \sqrt{(x_{cij} - x_f)^2 + (y_{cij} - y_f)^2 + z_f^2}
\]
and \(\varphi_{cij}\) is the phase shift due to the location of the unit-cell in the array
\[
\varphi_{cij} = -x_{cij}\sin\theta_c\cos\varphi_c - y_{cij}\sin\theta_c\sin\varphi_c
\]

4. Design of NDRA reflectarray antenna

The unit-cell of nano dielectric resonator reflectarray consists of an NDR made of titanium dioxide (TiO\(_2\)) with anisotropic frequency independent dielectric relative permittivity of 8.29 in x- and y-axis directions and 6.71 in z-axis direction, and estimated loss tangent of 0.001 [10]. The NDR has a cylindrical shape with radius \(R\) and height \(h_d\) placed on a square ground plane with thickness \(h\) to operate at 474 THz as shown in Fig. 4a. To calculate the required reflection coefficient phase compensation in each unit cell, the unit cell is put in a waveguide simulator [13]. The perfect electric and magnetic wall boundary conditions are posted onto the sides of the surrounding waveguide, and result in an infinite array. A linearly polarized plane wave was applied as the far-field excitation of the unit cells inside the waveguide simulator and only normal incidence angle is considered. There are several limitations to the infinite array approach. First, all elements of the reflectarray/transmitarray are identical; this is not the case in the real reflectarray/transmitarray in which the diameters of the NDR in each cell element must vary according to the required phase compensation. Second, the reflectarray/transmitarray itself is not infinite in extent. Finally, only normal incidence is considered. However, the plane wave has an oblique angle on the real array element, but the phase variation is nearly the same for incidence angles up to 30° [14]. Different metals are used for ground plane as silver, gold, copper, and aluminum. The properties of the ground plane metals are determined using Eq. (1) at 474 THz and are listed in Table I.

![Figure 3](image3.png)

Figure 3 The detailed structure of the reflectarray/transmitarray configuration.

![Figure 4](image4.png)

Figure 4 The detailed structure of the NDR reflectarray unit cell.

The required compensation phase of the reflection coefficient for each unit-cell is achieved by varying the NDRA radius \(R\). Figure 5 shows the variation of the reflection coefficient magnitude and phase versus the NDR radius at 474 THz for different ground plane metals. From the losses point of view the gold ground plane has the worst reflection coefficient (i.e. higher losses) variation from -30.4 dB to -2.9 dB, while the Silver ground plane gives the best reflection coefficient magnitude (i.e. lower losses) varies from -5.8 dB to -1.7 dB for the NDR radius varying from 85 nm to 170 nm. This is because the conductivity of the gold material is higher than that of the silver material at 474 THz as appeared in Fig1.b and the penetration in aluminum ground plate is higher than that of silver Fig. 2.
The phase of the reflection coefficient span of variation is 360° for the silver, 19° for gold, 215° for the copper, and 136° for the aluminum ground plate. The silver material has the best performance for the reflectarray unit-cell with reflection coefficient magnitude variation from -5.8 dB to -1.7 dB, and phase variation from 0 to 360°. Figure 6 shows the effect of changing the silver ground plane thickness (h) of the unit cell on the variation of the reflection coefficient magnitude and phase. By increasing the ground plane thickness (h), the reflection coefficient magnitude is decreased while the reflection coefficient phase variation is increased to achieve 360°.

A compromise between the magnitude and phase of the reflection coefficient has been made. A ground plane of thickness h=200 nm has been chosen for which the reflection coefficient magnitude varies from -1.7 dB to -5.8 dB and 360° phase variations. Silver ground plane with thickness h=200 nm has a slower phase variation than h=30nm which introduces a wider operating bandwidth and has a higher reflection coefficient magnitude in the area of interest of the NDR radius changes from R=105 nm to 170 nm. The electric field distribution on the unit-cell of the NDR reflectarray with silver supporting plane h=200 nm, h_d =50 nm, and R=130 nm is shown in Fig 7. The incident plane wave penetrates the silver supporting plane at a distance equal to the skin depth and reflects back to the source direction. The reflection occurs because the thickness (h) of the silver supporting plane is much bigger than the silver skin depth (about 8.16 δ).

Figure 5 The variations of the reflection coefficient magnitude and phase versus the NDR radius at 474 THz for the unit cell with different plane materials for h=200 nm, L=350 nm and h_d=50 nm.

Figure 6 The variations of the reflection coefficient magnitude and phase versus the NDR radius of the unit cell with silver supporting plane at different plate thickness h, at L=350 nm, h_d=50 nm.
A 21×21 unit cell NDRA reflectarray is simulated. Silver ground plane with \( L=350 \) nm, \( h=200 \) nm, and \( h_d=50 \) nm is considered as shown in Fig.8a. The phase distribution of the 21×21 unit cell is calculated using Eq. (7) as shown in Fig.8b. The array has total dimensions of 7.35×7.35 μm². A linearly polarized pyramidal nano-horn antenna is used to feed the NDRA reflectarray located at (0, 0, 8.133) μm from the array aperture in the horn phase centre. The nano-horn antenna is constructed from gold with \( L_a=487.5 \) nm, aperture size \( a \times b \) of 810 nm \( \times \)1275 nm, \( a_a \times b_a \) of 412.5 nm \( \times \)825 nm, and \( L_d=470.5 \) nm. The nano-horn antenna has a maximum gain of 11.1 dB at 474 THz. The E and H-plane radiation patterns at 474 THz of the nano-horn and the NDRA reflectarray with different ground plane thickness \( h=30, 70 \) and 200 nm are shown in Fig.9. For the inset variation from -10° to 10°, the maximum gain of the NDRA reflectarray is increased by increasing the ground plane thickness and the first side lobe level (SLL) is decreased. For \( h=200 \) nm the SLL is -15.1 dB and -17.9 dB in E-plane and H-plane respectively, and -23.3 dB in E-plane, and -14.8 dB in H-plane for nano-horn respectively. The half-power beamwidth (HPBW) of the NDRA reflectarray is 4.7° in E-plane and 4.5° in H-plane compared to 40.3° in E-plane and 41.3° in H-plane for the nano-horn antenna.

The 3-D radiation pattern of the reflectarray at \( f=474 \) THz of the NDRA reflectarray is shown in Fig.10a. The gain variations versus frequency for the NDRA reflectarray and the nano-horn are shown in Fig. 10b. The NDRA reflectarray has a maximum gain of 25.8 dB at 474 THz with 1-dB gain variation of 30 THz (from 459 THz to 489 THz).
than that of silver at 474 THz. The skin depth of silver at 474 THz is nearly 24.5 nm, where the transmitarray unit-cell thickness must have approximately twice the skin depth or less to maximize the transmission from the unit-cell. A compromise between the magnitude of the transmission coefficient and phase variation has been made. The electric field distribution on the unit-cell of the NDRA transmitarray with silver supporting plane, \( h=50 \) nm, \( h_d=50 \) nm and \( R=130 \) nm is shown in (Fig. 14). The incident plane wave passes to the other side silver supporting plane. The transmission occurs as the thickness of silver supporting plane is equal to twice the silver skin depth where the transmission condition is satisfied.

**5. Design of NDRA transmitarray antenna**

The NDRA transmitarray unit-cell consists of two NDRA placed on the opposite sides of the supporting plane as shown in Fig.11. Each NDRA has radius \( R \), height \( h_d \) and silver supporting plane with thickness \( h \) and length \( L \). The required compensation phase of the transmission coefficient for each unit-cell is accomplished by varying the NDR radius \( R \) using the wave guide simulator. Figure 12 shows the variation of the transmission coefficient magnitude and phase versus the NDR radius at 474 THz for \( L=350 \) nm, \( h=50 \) nm, \( h_d=50 \) nm for different supporting plane materials. The Aluminum supporting plane has the worst transmission coefficient variation from -26 dB to -17.3 dB, while the silver supporting plane gives the best transmission coefficient magnitude variation from -4 dB to -2.4 dB for the NDR radius variation from 85 nm to 170 nm. The phase of the transmission coefficient variation is 240° for gold, 300° for the copper, 350° for the silver and 180° for the Aluminum supporting plate. The silver material has the best performance for the transmitarray unit-cell with transmission coefficient magnitude variation from -4 dB to -2.4 dB and phase variation from 0 to 350°. The variation of the transmission coefficient magnitude and phase versus the NDRA radius for different silver supporting plane thickness of the unit-cell is shown in Fig.I.13. By increasing the supporting plane thickness the transmission coefficient magnitude is decreased. The skin depth of gold is greater...
A design of 17×17 unit-cells and a 21×21 unit-cells of the NDRA transmitarray at 474 THz are investigated. The element spacing between the unit cells is 350 nm, and supporting plane thickness \( h = 50 \) nm, \( h_d = 50 \) nm. The feeding horn is located at a distance \( F = 8.133 \) μm in the normal direction of the array plane. The E and H-plane radiation patterns at 474 THz for the 17×17 and the 21×21 NDRA Transmitarrays, and the horn antenna are shown in Fig. 16. For the 17×17 NDRA transmitarray, the SLL is -18.2 dB in E plane and -14.4 dB in H-plane respectively. The HPBW is 6.3° in E-plane and 5.8° in H-plane. For the 21×21 transmitarray, the SLL for is -18.2 dB in E plane and

-15.9 dB in H-plane. The HPBW of the transmitarray is 5.1° in E-plane and 4.8° in H-plane. The 3-D radiation patterns of the transmitarrays at \( f = 474 \) THz are shown in Fig.17a. The nano DRA transmitarray gain variation versus frequency is shown in Fig. 17b. The max gain is 23.9 dBi for 17×17 transmitarray and 27.5 dBi for 21×21 transmitarray and 11.2 dBi for nano horn antenna. The 1-dB band width is 55 THz (from 451.5 THz to 496.5 THz) for 17×17 transmitarray and 40 THz (from 460 THz to 500 THz) for 21×21 transmitarray. The E-plane and H-plane gain patterns for the 21×21 NDRA transmitarray at different frequencies are shown in Fig.18.

Figure 13 The variations of the transmission coefficient magnitude and phase versus the NDR radius with silver supporting plane thickness \( L = 350 \) nm, \( h_d = 50 \) nm.

Figure 14 The electric field distribution on the NDR transmitarray unit-cell with silver supporting plane \( h = 50 \) nm, \( L = 350 \) nm, \( h_d = 50 \) nm and \( R = 130 \) nm.

A design of 17×17 unit-cells and a 21×21 unit-cells of the NDRA transmitarray at 474 THz are investigated. The element spacing between the unit cells is 350 nm, and supporting plane thickness \( h = 50 \) nm, \( h_d = 50 \) nm. The feeding horn is located at a distance \( F = 8.133 \) μm in the normal direction of the array plane. The E and H-plane radiation patterns at 474 THz for the 17×17 and the 21×21 NDRA Transmitarrays, and the horn antenna are shown in Fig. 16. For the 17×17 NDRA transmitarray, the SLL is -18.2 dB in E plane and -14.4 dB in H-plane respectively. The HPBW is 6.3° in E-plane and 5.8° in H-plane. For the 21×21 transmitarray, the SLL for is -18.2 dB in E plane and

-15.9 dB in H-plane. The HPBW of the transmitarray is 5.1° in E-plane and 4.8° in H-plane. The 3-D radiation patterns of the transmitarrays at \( f = 474 \) THz are shown in Fig.17a. The nano DRA transmitarray gain variation versus frequency is shown in Fig. 17b. The max gain is 23.9 dBi for 17×17 transmitarray and 27.5 dBi for 21×21 transmitarray and 11.2 dBi for nano horn antenna. The 1-dB band width is 55 THz (from 451.5 THz to 496.5 THz) for 17×17 transmitarray and 40 THz (from 460 THz to 500 THz) for 21×21 transmitarray. The E-plane and H-plane gain patterns for the 21×21 NDRA transmitarray at different frequencies are shown in Fig.18.

Figure 15 (a) The detailed structure of the NDRA transmitarray with silver supporting plane, (b) side view, (c) The phase shift distribution of the NDRA transmitarray with the silver supporting plane.
Figure 16 The gain patterns for 21×21 NDRA transmitarray with silver supporting plane at 474 THz. $h=50$ nm, $L=350$ nm, and $h_d=50$ nm.

Figure 17 (a) The 3-D gain radiation pattern at $f=474$ THz. (b) The gain variation versus frequency for 17×17 and a 21×21 NDRA transmitarray with silver supporting plane.

Figure 18 The gain radiation patterns for a 21×21 NDRA transmitarray with silver supporting plane at different frequencies.

6. Conclusion

The use of NDR in the design of nano-reflectarray and nano-transmitarray for terahertz application at 633 nm is introduced. The reflectarray unit cell consists of a cylindrical NDR on a square ground plane of a good conductor. A parametric study for the unit cell dimensions optimization has been introduced. The gold ground plane has got the worst reflection coefficient (higher losses), while the silver ground plane gives the best reflection coefficient magnitude. Silver ground plane with thickness of 200 nm has been chosen for reflection coefficient magnitude varies from -1.7 dB to -5.8 dB and 360° phase variation. The silver ground plane with thickness 200 nm introduces slower phase variation and hence wider bandwidth. The NDRA reflectarray consists of 21×21 unit cells with a silver ground plane of $L=350$ nm, $h=200$ nm, and $h_d=50$ nm is simulated using the full-wave simulator. The maximum gain of the NDRA reflectarray is increased by increasing the ground plane thickness and the SLL is decreased. The NDRA reflectarray introduces a maximum gain of 25.8 dB at 474 THz with 1-dB gain variation bandwidth of 30 THz. The NDRA transmitarray unit-cell consists of two NDRA placed on both sides of the supporting plane, has been designed and analyzed. The Aluminum ground plane has the worst transmission coefficient variation from -26 dB to -17.3 dB.
The silver as a supporting plane material has shown the best characteristics when compared with gold, copper, and aluminum. Comparison between transmitarray with 17×17 unit-cells and of 21×21 unit-cells at 474 THz have been introduced. The maximum gain is 23.9 dB for the 17×17 transmitarray and 27.5 dB for the 21×21 transmitarray while 11.2 dB for the feeding nano horn antenna.

References